

The Solar Neutrino Puzzle

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Birth of the Neutrino

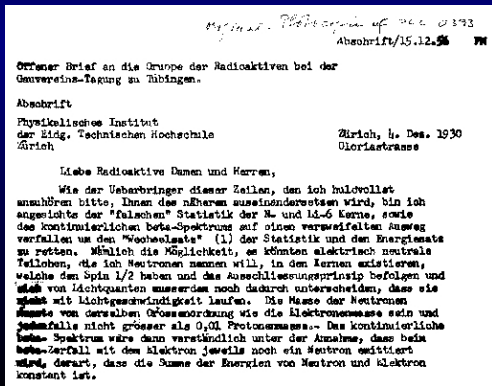
Problem (Chadwick & Ellis, 1914) in β decay $N \rightarrow N' + e^-$:
the electron energy spectrum is **continuous**! For a general two-body
decay $A \rightarrow B + C$ it is straightforward to compute that the energy of
particle B is given by

$$E_B = \frac{(m_A^2 + m_B^2 - m_C^2)c^2}{2m_A}$$

hence the energies are **fixed**.
But only N' , e^- observed?!

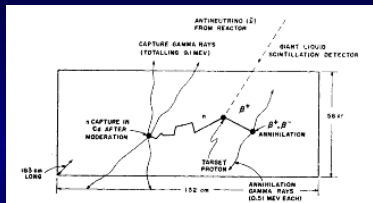
Pauli (1930): assume
existence of a **neutral**,
spin-1/2 particle (spin
discovered in 1925) with mass
 $m \ll m_p$: the **neutrino** ν^\ddagger

\ddagger after Chadwick (1932) claimed
the name "neutron"



Neutrinos and Anti-Neutrinos

Anti-neutrinos (defined as the particles liberated in the fission of neutron-rich uranium, *i.e.*, $n \rightarrow p + e^- + \bar{\nu}_e$) were observed first by Reines and Cowan (1959) at the Savannah River nuclear power plant.



With $10^{13} \text{ cm}^{-2} \text{ s}^{-1}$: 36 interactions per hour! Very low rates observable at all (on top of backgrounds) due to specific experimental signature

Anti-neutrinos were identified in this experiment through the reaction $\bar{\nu}_e + p \rightarrow n + e^+$:

- β^+ radiation: annihilation with electrons \Rightarrow two 511 keV photons
- neutron capture by Cd, followed by de-excitation: *delayed* coincidence

Davis and Harmer (1959) looked for $\bar{\nu}_e + {}^{37}\text{Cl} \rightarrow {}^{37}\text{Ar} + e^-$ but did **not** observe it

Neutrinos and anti-neutrinos are **different particles!**

Birth of Particle Physics

Since V. Hess's balloon flights in 1912: **cosmic rays**
(seen here in emulsion: energy loss by charged particles used to visualize their trajectories)



Yet another source of “missing momentum”!

Interpretation (Powell *et al.*, 1947): decays of new particles

- $\pi^\pm \rightarrow \mu^\pm \nu$
- $\mu^\pm \rightarrow e^\pm \nu \nu$

Many more (generally heavier) particles have been discovered in cosmic rays.

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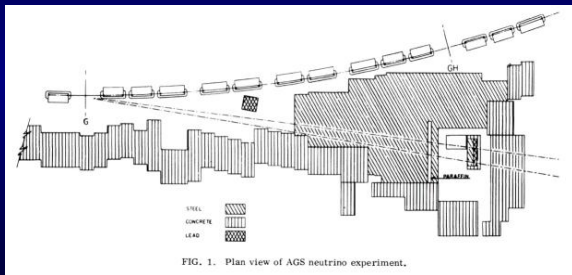
Many more (generally heavier) particles have been discovered in cosmic rays. Quoting from Lamb's (1955) Nobel speech:

“the finder of a new elementary particle used to be rewarded by a Nobel Prize, but such a discovery now ought to be punished by a \$10,000 fine”

Neutrino Types

With the advent of high-energy particle accelerators (since early fifties), **controlled** experiments have become possible. Example:

If there were only one type of neutrino, high-energy ν would lead to the production of muons and electrons in similar amounts. This was tested in the early 60's at the AGS in Brookhaven using **neutrinos from π^\pm decay**



Observation: only muons were produced \Rightarrow
there is more than one neutrino type: $\nu_\mu \neq \nu_e$

What have we learned?

A selection of important results. . .

- most particles discovered in cosmic ray events and (later) in accelerator-based experiments are **not** “fundamental” but composite particles, consisting of **quarks** (and/or anti-quarks)
 - this is true for p, n (but **not** for the electron)
- there appear to be four fundamental forces or **interactions** in Nature:
 - gravity: this holds our feet on the ground, Earth in its orbit around the Sun, etc.
 - electromagnetism: responsible for the most “visible” phenomena (**all** molecular interactions, existence of solids and liquids, . . .)
 - strong interaction: needed to hold protons and neutrons together in nuclei – but **also** the quarks in a proton or neutron
 - weak interaction: responsible for a large fraction of the possible nuclear transmutation processes, and in particular for **fusion processes in the Sun and other stars**

The Standard Model

The Standard Model of particle physics (Glashow, Salam, Weinberg, '67) captures our collected wisdom about particles and their interactions:

Matter particles (for each particle there is a corresponding antiparticle):

	charge	family 1	family 2	family 3
leptons	0	$\begin{pmatrix} \nu_e \\ e^- \end{pmatrix}$	$\begin{pmatrix} \nu_\mu \\ \mu^- \end{pmatrix}$	$\begin{pmatrix} \nu_\tau \\ \tau^- \end{pmatrix}$
quarks	$+2/3e$	$\begin{pmatrix} u \\ d \end{pmatrix}$	$\begin{pmatrix} c \\ s \end{pmatrix}$	$\begin{pmatrix} t \\ b \end{pmatrix}$

Interactions are not “instantaneous” (this would violate Special Relativity) but are **mediated by so-called gauge bosons**:

electromagnetism: **photon** (light!)

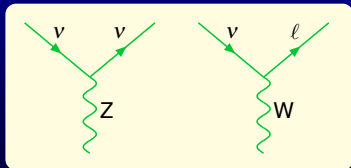
strong interaction: **gluons**

weak interactions: **Z, W[±]**

More on Interactions

Knowing the interactions allows us to compute relevant quantities (lifetimes of unstable particles, interaction cross sections). The various couplings can be represented graphically using **Feynman diagrams** (which are useful also for these computations). Example:

The neutrinos only interact with the Z and W^\pm bosons mediating the weak interaction:



- the interaction with the Z (W^\pm) boson is also called **Neutral Current** (**Charged Current**)
- the weak interaction is “weak” because the Z , W^\pm are heavy!
(in contrast to the massless γ , g)

“Building blocks” such as these can be used to construct complete interaction processes

Outstanding Questions

- ① How can we be massive?
 - ⇒ the fact that particles (leptons, quarks, but also the W and Z bosons) can have mass at all is as yet unexplained. We have a working hypothesis (the Higgs mechanism) but it implies the existence of a thus far unobserved particle: the **Higgs boson**

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- 4 Are neutrinos their own anti-particles?
⇒ this is not possible for other matter particles, but it would help greatly to address the previous issue

The High-Energy Frontier

In a few months from now,
the Large Hadron Collider at
CERN (Geneva) will start
operation

- 1 accelerate intense
beams of protons to
energies of 7 TeV
($v = 0.9999991c$)
- 2 make these protons
collide head-on in the
centre of a detector
- 3 observe the outcome of
the interactions

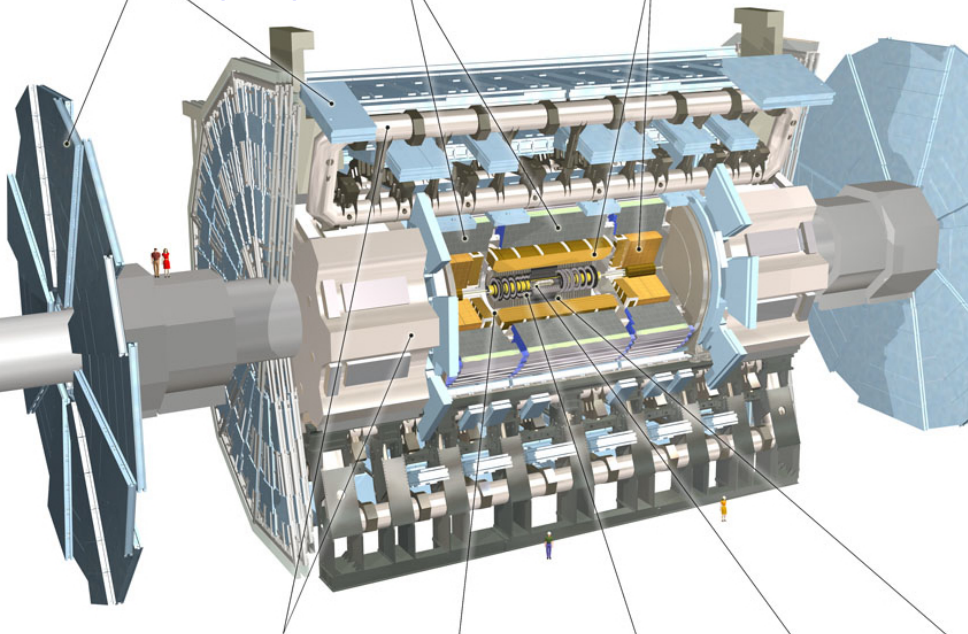
Aim: find new particles like the Higgs boson or evidence of
Supersymmetry, and walk away with a Nobel Prize

Muon Detectors

Tile Calorimeter

Liquid Argon Calorimeter

No Table-Top Experiments!



Toroid Magnets

Solenoid Magnet

SCT Tracker

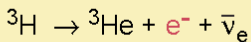
Pixel Detector

TRT

Neutrino Masses: experiment

Decay kinematics have been used for half a century to try and measure neutrino masses: the electron energy spectrum (mostly for ^3H decay)

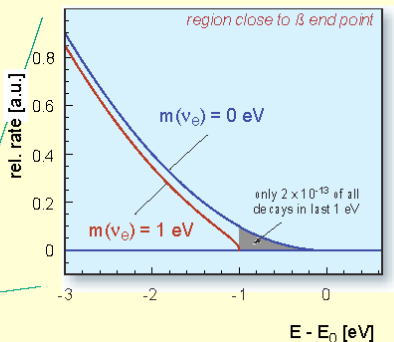
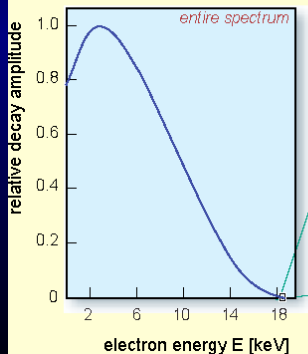
tritium β -decay and the neutrino rest mass



superallowed

half life : $t_{1/2} = 12.32 \text{ a}$

β end point energy : $E_0 = 18.57 \text{ keV}$



Neutrino Masses: experiment

The latest attempt is the Karlsruhe tritium neutrino (KATRIN) experiment:
expected sensitivity ~ 0.2 eV

arrival of KATRIN spectrometer



The Sun



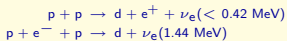
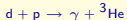
What makes stars like our Sun shine?

- 1 accretion of mass
- 2 collapse due to gravitation
- 3 increase of pressure and temperature \Rightarrow

Ignition of stellar burning: nuclear fusion

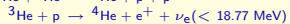
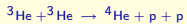
These processes are **known** and part of the **Standard Solar Model** (Bahcall et al.) dating from the 60's but refined since then

Primary Fusion Processes in the Sun

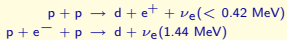
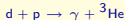


pp I cycle: 86% of solar ν

hep: 10^{-7} of solar ν

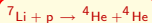
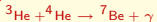
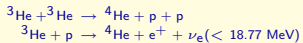


Primary Fusion Processes in the Sun

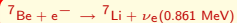


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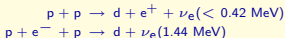
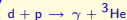
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pp II cycle: 14% of solar ν

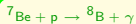
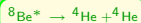
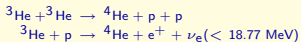


Primary Fusion Processes in the Sun

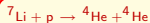
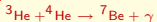
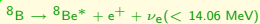


pp I cycle: 86% of solar ν

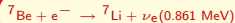
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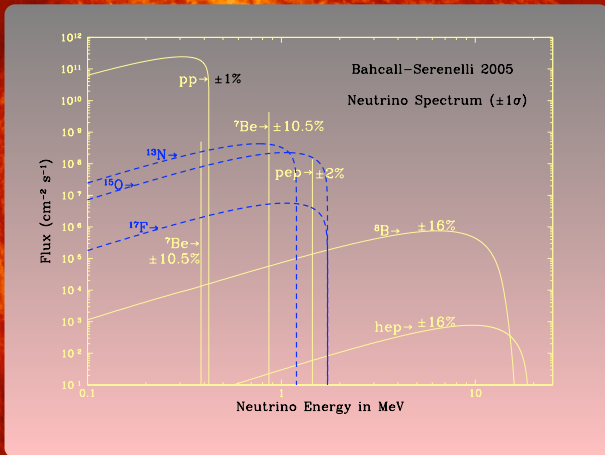
pp III cycle: $1.5 \cdot 10^{-4}$ of solar ν



pp II cycle: 14% of solar ν

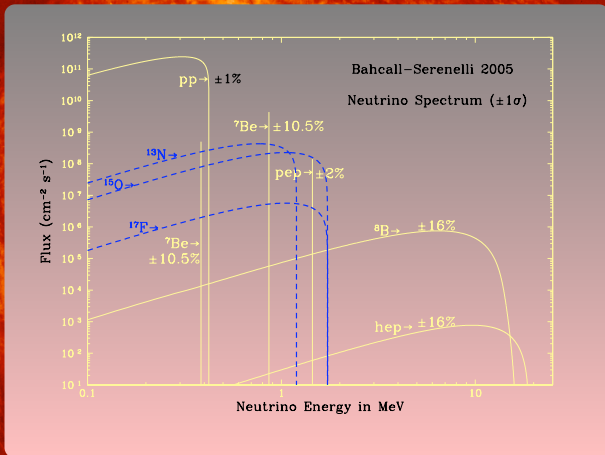


The Resulting Neutrino Spectrum



Total neutrino flux on Earth: $\sim 6 \cdot 10^{10} \text{cm}^{-2} \text{s}^{-1}$ (!!!)

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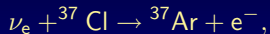


Total neutrino flux on Earth: $\sim 6 \cdot 10^{10} \text{cm}^{-2} \text{s}^{-1}$ (!!!)
... but don't worry: < 1 interaction/s per human body

The Homestake Experiment

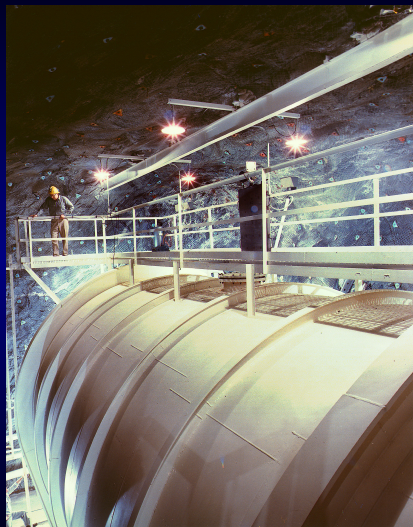
Ray Davis set out ('64) to test the Standard Solar Model's predictions.

- **radiochemical**: capture process



$$E_\nu > 0.814 \text{ MeV } ({}^7\text{Be } \nu_e)$$

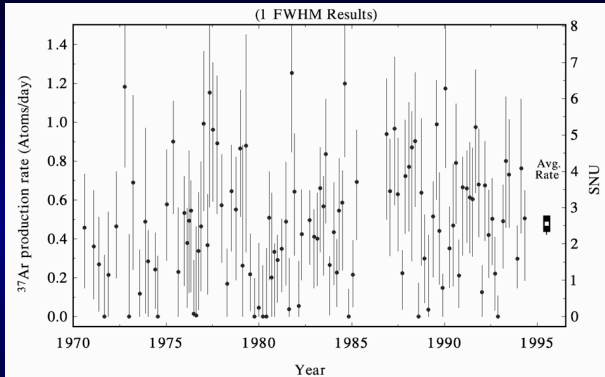
- with 400,000 l C_2Cl_4 : expected to observe 1.5 interaction per day
- Homestake gold mine (South Dakota): **1.5 km depth** to shield the experiment from backgrounds
- painstaking procedure to filter ${}^{37}\text{Ar}$ atoms and observe their decays



An experiment that lasted 35 years!

The Homestake Experiment

Results from the experiment: only $\sim 1/3$ of the expected flux observed



Clearly, there was a problem. But where: in the **physics**, the **measurement**, or in the **flux predictions**?

- Later, other radiochemical experiments ($^{71}\text{Ga} + \nu_e \rightarrow ^{71}\text{Ge} + e^-$, $E_\nu > 0.232 \text{ MeV}$) also observed deficits (observed fraction ~ 0.55)

The Standard Solar Model

So why would one doubt the validity of the SSM predictions? The SSM needs to describe temperature, pressure, density, composition, all as a function of radius.

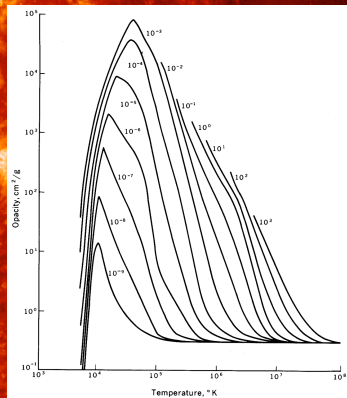
But we only observe the outside!

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But we only observe the outside!

- Part of it is really simply physics...
 - relations between density profile and pressure, etc.
- But in particular the **temperature profile** depends very much on absorption in the Sun's atmosphere
 - this itself depends on a detailed knowledge of microscopic physics processes, as well as composition
 - these are partly calculated and partly measured in the laboratory
- And the ${}^7\text{Be}$ and ${}^8\text{B}$ ν production processes depend on temperature as T^{11} and T^{25} , respectively!



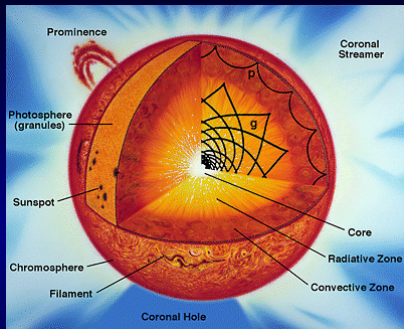
curves for different ρ

Helioseismology to the Rescue

The Sun's surface is not static!

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Sound waves of different **angular momentum** probe the density at different radii!

The density profile as measured using **helioseismology** is in good agreement with the SSM predictions

The Neutrino Oscillation Formalism

The Standard Model *does* in fact allow for massive neutrinos

- fermion masses are generated **dynamically** through an interaction with the Higgs field: this interaction need not be “flavour diagonal”
- the resulting mass matrix can be diagonalized, so as to yield **mass eigenstates** which are linear superpositions of **flavour eigenstates**:

$$\nu_i = \sum_{\alpha} U_{i\alpha} \nu_{\alpha}$$

All this is *exactly* analogous to the well-known phenomenon of **quark mixing**, but with two important practical differences:

- 1 unlike quarks, neutrinos exist as free particles
- 2 the neutrino masses (and therefore also the mass differences) are much smaller \Rightarrow neutrinos propagate **coherently** over macroscopic (even astronomic) distances

The Neutrino Oscillation Formalism

If now a ν_e of given momentum p is created at time $t = 0$, the **amplitude** that at some later time t it will still manifest itself as a ν_e is

$$A_{ee} \equiv A(\nu_e \rightarrow \nu_e) = \sum_i U_{ie}^* e^{-iE_i t / \hbar} U_{ie}$$

In quantum mechanics, it's the **square** of the amplitude that matters!

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For simplicity, consider only two neutrino species, and

$$U = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix}$$

For ultrarelativistic neutrinos, one can approximate

$$E_i = \sqrt{p^2 c^2 + m_i^2 c^4} \approx pc + \frac{m_i^2 c^3}{2p}$$

Filling in all the numbers, one obtains

$$\begin{aligned} P_{ee} &= |A_{ee}|^2 \\ &\approx 1 - \sin^2 2\theta \sin^2 \left(\frac{(m_1^2 - m_2^2)c^3 t}{4p\hbar} \right) \\ &\approx 1 - \sin^2 2\theta \sin^2(1.27 \Delta m^2 L/E) \end{aligned}$$

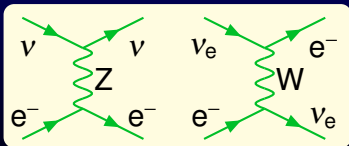
(E in GeV, L in km, m^2 in eV^2)

Small Δm^2 require large L !

The SNO Principle

Basic reactions in normal matter:

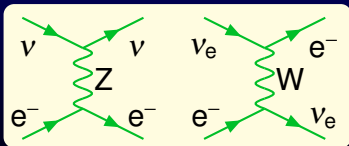
- CC: $\nu_e + n \rightarrow e^- + p$
(this works only for ν_e : the ν are not sufficiently energetic to produce μ or τ)
- NC: $\nu + n, p \rightarrow \nu + n, p$
(for all three ν)
- ES: $\nu + e^- \rightarrow \nu + e^-$
(possible for all three ν , but cross section for $\nu_e \sim 6$ times as high as for ν_μ, ν_τ)



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From the proposal by H. Chen (1985):

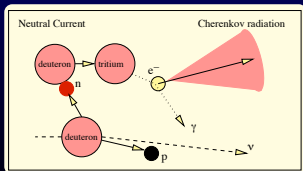
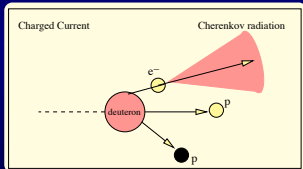
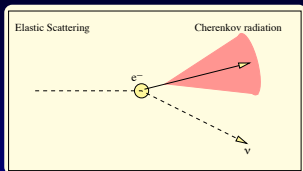
An experiment which directly addresses the solar-neutrino problem should be sensitive to all neutrino species equally. Such a measurement could determine the total solar-neutrino flux *even if neutrinos oscillate*.

- we need an experiment that can measure **Neutral Current** as well as Charged Current events
- ... but the ν usually carries most of the energy \Rightarrow **very** hard to observe!
- the exception: ν -induced disintegration of the **deuteron**

Use heavy water: D_2O

The Detection Strategy

The three different interactions manifest themselves differently:



ES: an electron receives a significant amount of energy and travels roughly in the direction of the incoming ν_e . It loses energy mainly through Cherenkov radiation (\sim shock wave).

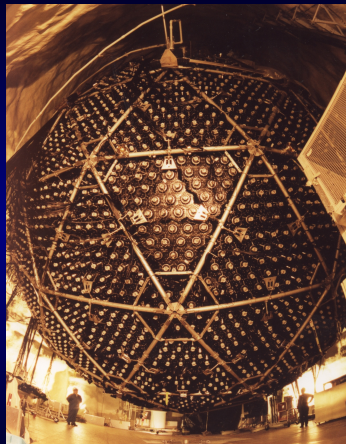
CC: the neutrino is transformed to a (high-energy) electron (but \sim without the directional correlation). The protons remain undetected.

NC: the neutrino splits the deuteron, and the liberated neutron leads to the formation of an excited triton. The triton decays to its ground state through the emission of a 6.25 MeV photon. The photon collides with atomic electrons.

Down to Earth

The Sudbury Neutrino Observatory: design

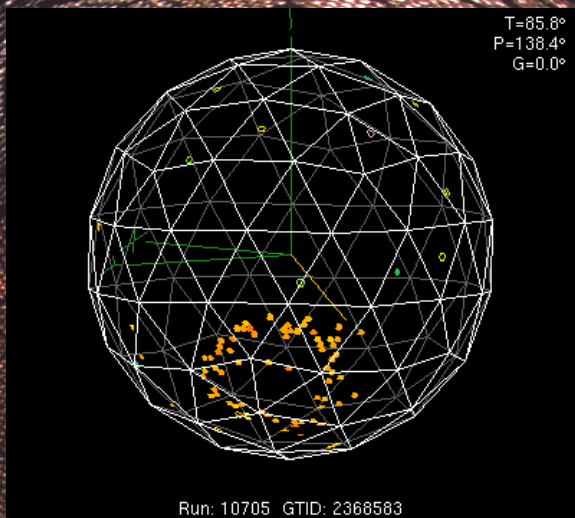
- **heavy water**: available in large quantities in Canada (but representing \sim Cnd\$ 300M, on loan from AECL)
- **radiation free environment**: as in the Homestake experiment, the experiment is quite susceptible to other sources of radiation than neutrinos (radioactive materials, decays from cosmic rays)
 \Rightarrow 2 km underground!
- **good photodetection capabilities**: use \sim 10,000 PMTs of diameter 20 cm to cover the inside of a 12 m diameter acrylic vessel



Support structure with PMTs

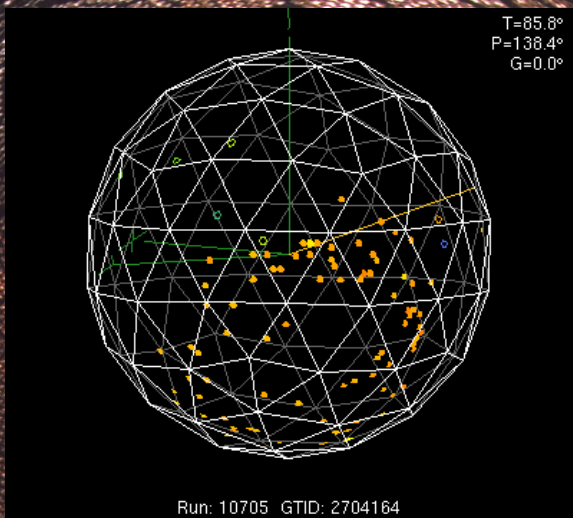
Some Candidate Events

Colour coding: PMT hit time relative to trigger timestamp



Some Candidate Events

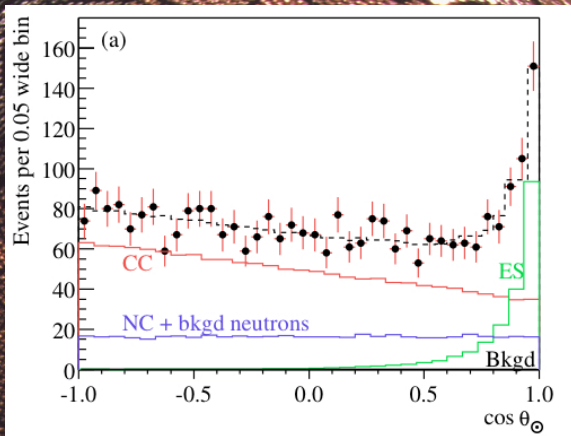
Colour coding: PMT hit time relative to trigger timestamp



Results: event distributions

The three interactions can be distinguished only statistically!

- Angle between Cherenkov cone direction and the Sun

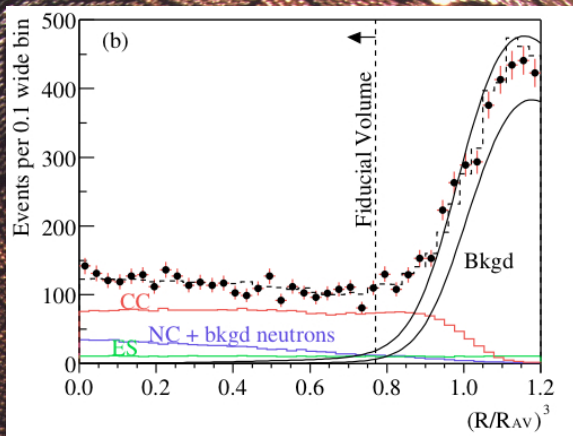


It is assumed that the **shapes** of the distributions for the different processes are known; their relative contributions are fit

Results: event distributions

The three interactions can be distinguished only statistically!

- Radial coordinate of the reconstructed interaction point

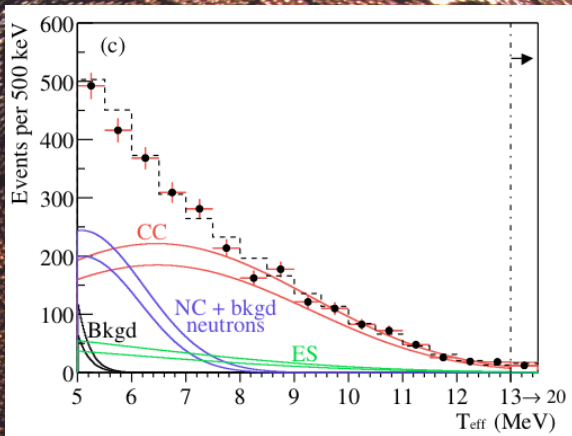


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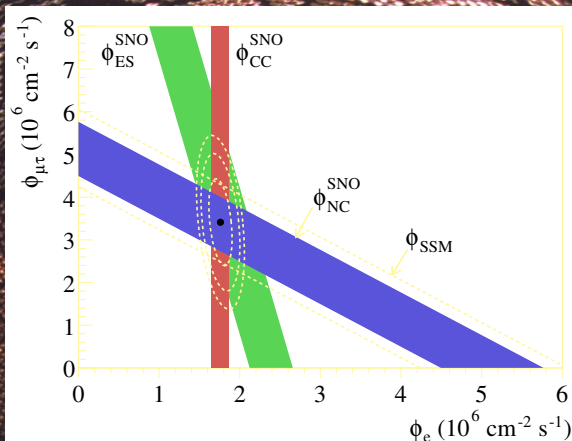
- Reconstructed energy



It is assumed that the **shapes** of the distributions for the different processes are known; their relative contributions are fit

Evidence for Oscillations

Using the total cross sections for the individual processes, a flux determination can be made:



The data are incompatible with the absence of $\nu_{\mu}, \nu_{\tau} \Rightarrow$
evidence for neutrino oscillations!

Missing Details

This talk isn't complete!

- I haven't mentioned the **atmospheric neutrino anomaly**: a deficit of $\nu_\mu, \bar{\nu}_\mu$ in decay chains of cosmic rays impinging on the atmosphere. This provided the first indication for neutrino oscillations (Super-Kamiokande, 1998)

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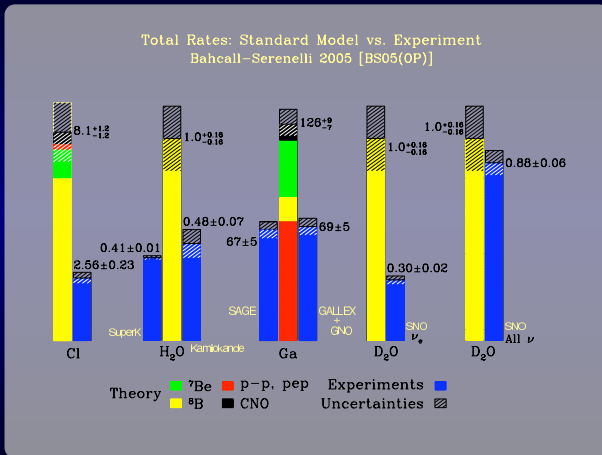
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- Using only oscillations in vacuum, it isn't possible to explain $P_{ee} < 0.5$. This needs the Mikheyev-Smirnov-Wolfenstein or **MSW** effect, affecting the propagation of neutrino states in matter due to the presence of (large densities of) electrons
 - this explains why the Gallium experiments found a smaller deficit (on average, smaller E_ν)

Bottom Line

Compare again the measurements with theory predictions:



Very satisfactory agreement!

Conclusions

- The Standard Solar Model has withstood 40 years of scrutiny
 - the (total) observed ν flux is now used to estimate the temperature in the Sun's core!
- SNO (and Super-Kamiokande) have convinced the world that neutrino oscillations are for real!
- A deeper understanding of the nature of neutrinos may be the key to understanding the matter–antimatter asymmetry
 - information may come either from the high-energy frontier (LHC) or from experiments conducting dedicated studies of neutrinos